

GRADE : 11

DATE : 2 / 6 / 2014

SUBJECT : Mathematics

TITLE : Paper I

EXAMINER : ~~Mrs A. Slaughter~~ Mrs Selkirk

TOTAL MARKS : 100

TIME : 2 hour(s)

SOLUTIONS

1.1.1	$x^2 - x - 20 = 0$ ✓ std form $(x - 5)(x + 4) = 0$ ✓ factors $x = 5$ or -4 ✓ (both)	3	1.1.5	$x^3 - x = 0$ ✓ std form $x(x^2 - 1) = 0$ $x(x - 1)(x + 1) = 0$ ✓ factors $\therefore x = 0$ or -1 or $+1$ ✓ (all)	3
1.1.2	$3x^2 - 2x - 4 = 0$ ✓ std form $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ ✓ formula $x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(-4)}}{2(3)}$ ✓ subst $x = 1,54$ or $-0,87$ ✓	5	1.1.6	$(3^x - 9)(3^x - 1) = 0$ ✓ $3^x = 9$ or $3^x = 1$ ✓ both $\therefore 3^x = 3^2$ or $3^x = 3^0$ $x = 2$ ✓ or $x = 0$ ✓	4
1.1.3	$\sqrt{2 - x} = 4 + x$ ✓ isolate $\sqrt{\quad}$ $2 - x = x^2 + 8x + 16$ ✓ square both sides $x^2 + 9x + 14 = 0$ ✓ std form $(x + 7)(x + 2) = 0$ ✓ factors $\therefore x = -7$ or -2 ✓ reject -7 [-1 if -7 not rejected]	5	1.1.7	$x^3 - 5x^2 + 4x > 0$ ✓ $x(x^2 - 5x + 4) > 0$ $x(x - 4)(x - 1) > 0$ ✓ factor $\frac{-}{-} \frac{+}{+} \frac{-}{-} \frac{+}{+}$ $0 \quad 1 \quad 4$ $x \in (0; 1) \text{ or } (4; \infty)$ ✓ [-1 no "or"]	4
1.1.4	$x^{-3/2} = \frac{32}{5}$ or -4 ✓ (both) $x = \left(\frac{32}{5}\right)^{-2/3}$ ✓ $x = 0,29$ ✓ No solution ✓	4	1.1.8	$3^x(x - 5) < 0$ $3^x > 0$ always ✓ $\therefore x < 5$ ✓ [Answer only = full marks] $\ominus \quad 0 \quad +$ $\quad \quad \quad 5$	2
				$3^x = 0$ no soln. \therefore no contribution	

1.2.	$y = 2x - 2$ ✓			$= \frac{6(2\sqrt{2} - \sqrt{3} \cdot \sqrt{2})}{6}$	
	Sub: $2x - 2 = x^2 - x - 6$ ✓			$= 2\sqrt{2} - \sqrt{3} \cdot \sqrt{2}$ ✓	6
	$x^2 - 3x - 4 = 0$ ✓ std form				[10]
	$(x - 4)(x + 1) = 0$ ✓ factors				
	$\therefore x = 4$ or $x = -1$ ✓ both	3.1.1	$x = 2$ ✓		1
	$\therefore y = 6$ or $y = -4$ ✓	3.1.2	$x - 1 \geq 0$ ✓		
			$\therefore x \geq 1$ ✓ but $x \neq 2$		2
1.3	$x^2 - x - 2 = 0$ [÷ -2] ✓	3.2.1	$\Delta = (-2)^2 - 4(8)(-1)$ ✓ Subst		
	$x^2 - x = 2$ ✓		$= 36$ ✓		2
	$x^2 - x + (-\frac{1}{2})^2 = 2 + (-\frac{1}{2})^2$ ✓	3.2.2	Real, Rational and unequal ✓		3
	$(x - \frac{1}{2})^2 = 2\frac{1}{4}$ ✓				
	$x - \frac{1}{2} = \pm \sqrt{9\frac{1}{4}}$ ✓				
	$x = \frac{1}{2} \pm \frac{3}{2}$ ✓	3.3	$mx^2 - x^2 + 2x - m + 3 = 0$		
	$\therefore x = 2$ or -1 ✓ both [4.4]		$(m - 1)x^2 + 2x + 3 - m = 0$ ✓ std form		
	[∴ must be shown or 0 for line 2]		$\Delta = (2)^2 - 4(m - 1)(3 - m)$ ✓ Subst		
2.1	$\sqrt{49 \times 2} \cdot (\sqrt{25 \times 2} - \sqrt{9 \times 2})$ ✓		$= 4 - 4(4m - 3 - m^2)$ ✓		
	$= 7\sqrt{2} (5\sqrt{2} - 3\sqrt{2})$ ✓		$= 4m^2 - 16m + 16$ ✓		
	$= 7\sqrt{2} (2\sqrt{2})$ ✓		$= 4(m - 2)^2$ ✓		
	$= 14 \cdot 2$				
	$= 28$ ✓	4	$(m - 2)^2 \geq 0$ for all $m \in \mathbb{R}$		
2.2.	$9 - 6\sqrt{3} + 3$ ✓		$\therefore 4(m - 2)^2 \geq 0$ ✓		
	$\frac{\sqrt{3} \times \sqrt{3} \times 2}{\sqrt{3} \times \sqrt{3} \times \sqrt{2}}$ [Must be shown or (5.1)]		$\therefore \Delta \geq 0$		
	$= \frac{12 - 6\sqrt{3}}{\sqrt{3} \times \sqrt{3} \times \sqrt{2}}$	4.1	\therefore Roots will always be real. ✓		5
	$= \frac{12 - 6\sqrt{3}}{3\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$ ✓ must be shown				[13]
	$= \frac{12\sqrt{2} - 6\sqrt{3} \cdot \sqrt{2}}{3 \cdot 2}$	4.2.1	1st diff: $4(1) + 6 = 10$ ✓		
			2nd $4(2) + 6 = 14$ ✓		
			3rd $4(3) + 6 = 18$ ✓		3

4.1. $-46; -67$ ✓✓ 2
 4.2.1. $10; 14; 18$ ✓✓✓ 3

4.2.2. 1. $T_2 \quad T_3 \quad T_4$
 $\begin{array}{ccc} \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} \\ 10 & 14 & 18 \\ & \underbrace{\quad} & \underbrace{\quad} \\ & 4 & 4 \end{array}$
 $2a = 4$ ✓✓
 $a = 2$ ✓✓

4.2.3. $3a + b = 10$ ✓✓
 $b = 4$ ✓✓
 $2 + 4 + c = 1$
 $a + b + c = 1$ ✓✓
 $c = -5$ ✓✓

5.1. $(5 \cdot 3)^{1-n} \times 5^{n+1} \times (3^4)^{-1}$
 $(2^2)^{n+2} \times (3^2 \cdot 2^2)^{-n-1}$
 ✓✓ x brackets [-1 per error]
 $= 5^{1-n} \cdot 3^{2-2n} \cdot 5^{n+1} \cdot 3^{-4}$
 $2^{2n+4} \cdot 3^{-2n-2} \cdot 2^{-2n-2}$
 $= \frac{5^0 \cdot 3^{-2-2n}}{2^2 \cdot 3^{-2n-2}}$
 $= \frac{1}{4}$ ✓✓

5.2. $\frac{2^{2n} - 2^2 \cdot 2^n + 4}{2^n - 2}$
 $= \frac{2^{2n} - 4 \cdot 2^n + 4}{2^n - 2}$
 $= \frac{(2^n - 2)(2^n - 2)}{2^n - 2}$ ✓ factors
 $= 2^n - 2$ ✓

6. On Diagram Sheet. [7]

7.1. Sub (1;4): $4 = 2a^{-1}$ ✓ subst
 $2 = a^{-1}$
 $(2)^{-1} = (a^{-1})^{-1} \quad 2 = \frac{1}{a}$ ✓
 $a = \frac{1}{2}$
 $\therefore f(x) = 2 \left(\frac{1}{2}\right)^x$

7.2. Sub $x=0$: $y = 2 \left(\frac{1}{2}\right)^0$
 $= 2$
 $\therefore (0; 2)$ Not given as coords = 0/2 ✓✓

7.3. $g(x) = 2 \left(\frac{1}{2}\right)^{-x}$
 OR $= 2 \cdot 2^x$ any one ✓
 OR $= 2^{x+1}$
 $= 2a^{-x}$

7.4. See diagram Sheet A

$u = 2 \left(\frac{1}{2}\right)^{x-1} - 4$
 let $x=0$: $y = 2 \left(\frac{1}{2}\right)^{-1} - 4$
 $= 2 \cdot 2 - 4$
 $= 0$
 $\therefore y$ -int $(0; 0)$

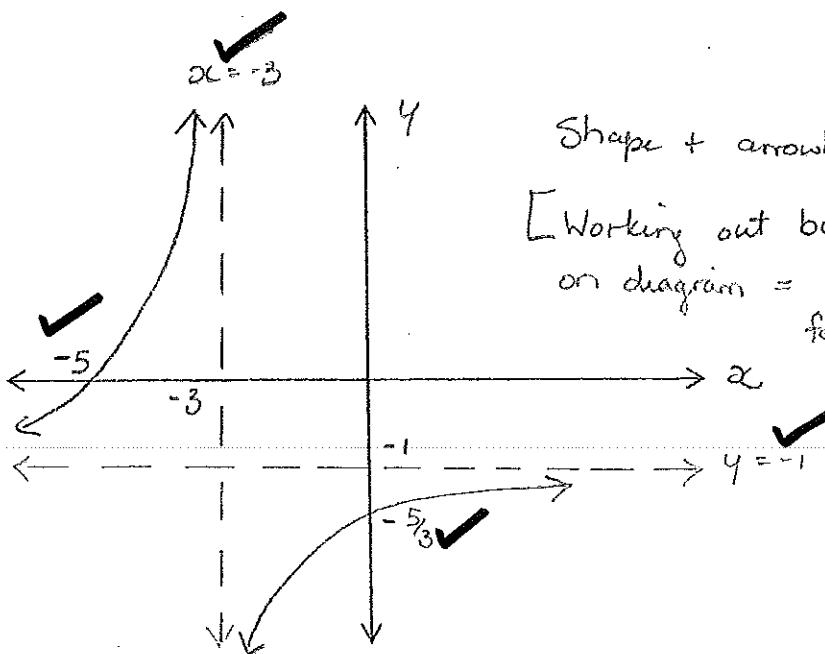
New asymptote at $y = -4$. 3

[8]

Diagram Sheet A

Question 6

6.1



Shape + arrowheads ✓
 [Working out but not indicated on diagram = 0 for that feature of x -int.]

5

(5)

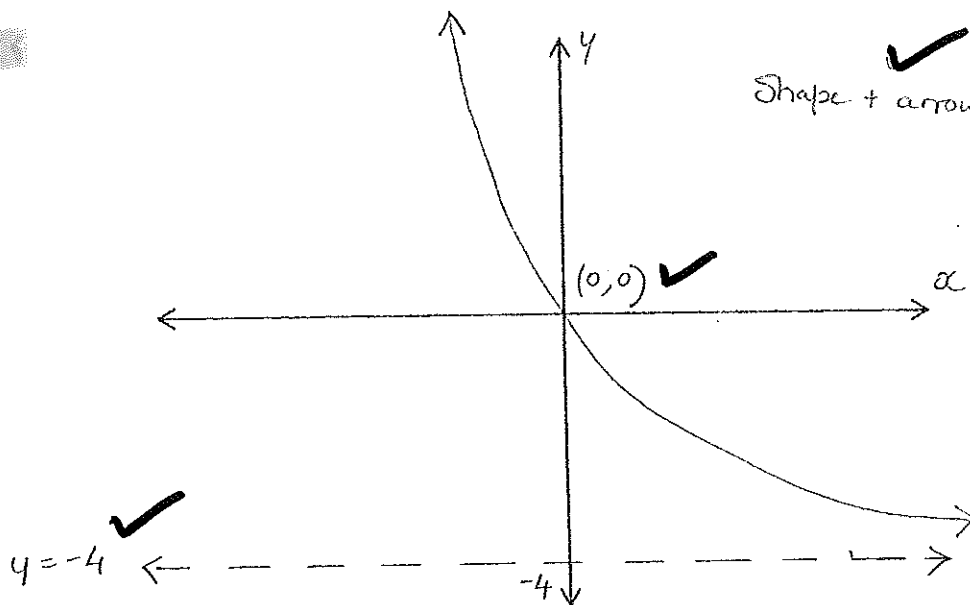
6.2

$y = -x - 4$

(2)

Question 7

7.4



Shape + arrowheads ✓

3

(3)